

The root of a polynomial in new notation

The root of a polynomial can be understood in the following:

(1) The equation $x^2 - 4 = 0$ can be solved as $x = \pm 2$. While we try to solve the equation $x^2 - 3 = 0$ we cannot solve it in rational field. The method to find the root is to introduce a new notation $x = \pm\sqrt{3}$. the general notation is n -th root $x = \sqrt[n]{r}$

The notation n -th root can write the root of a polynomial if the degree of power less or equal to 4.

(2) If the power of a polynomial great or equal than 5 we cannot write the root in the n -th root notation $x = \sqrt[n]{r}$.

Our conjecture is if we introduce new notation

$$\text{The root of equation } x^n - (px + q) = 0 \text{ is } x = \sqrt[n]{(p, q)}$$

We can use this notation to write the root of equation $x^n + a_1x^{n-1} + \dots + a_{n-1}x + a_n = 0$.

Maybe we need general notation

$$\text{The root of equation } x^n - (px^2 + qx + r) = 0 \text{ is } x = \sqrt[n]{(p, q, r)}$$

if the power of polynomial is higher

Liu Shenquan

Professor of Department of Mathematics,

South China University of Technology,

Guangzhou, China, 510640

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